A Theta-Band EEG Based Index for Early Diagnosis of Alzheimer’s Disease

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Abstract. Despite recent advances, early diagnosis of Alzheimer’s disease (AD) from electroencephalography (EEG) remains a difficult task. In this paper, we offer an added measure through which such early diagnoses can potentially be improved. One feature that has been used for discriminative classification is changes in EEG synchrony. So far, only the decrease of synchrony in the higher frequencies has been deeply analyzed. In this paper, we investigate the increase of synchrony found in narrow frequency ranges within the θ band. This particular increase of synchrony is used with the well-known decrease of synchrony in the δ band to enhance detectable differences between AD patients and healthy subjects. We propose a new synchrony ratio that maximizes the differences between two populations. The ratio is tested using two different data sets, one of them containing mild cognitive impairment patients and healthy subjects, and another one, containing mild AD patients and healthy subjects. The results presented in this paper show that classification rate is improved, and the statistical difference between AD patients and healthy subjects is increased using the proposed ratio.

Keywords: Alzheimer’s disease, data interpretation, electroencephalography, mild cognitive impairment, phase synchronization

INTRODUCTION

Alzheimer’s disease (AD) is the most common type of dementia. It is characterized by cognitive deficits and behavioral disturbances. AD starts with difficulties to remember new information, and then individuals experience other difficulties as the disease progresses [1]. There is currently no cure for this disease, though several medications are believed to delay the symptoms [2]. An early diagnosis of AD is considered a key factor that could benefit patients in early stages of the disease, i.e., mild cognitive impairment (MCI) or mild AD.

In order to develop a system for an early diagnosis of AD, the potential of a recording technique known as electroencephalography (EEG) has been investigated. EEG consists in recording brain-related electrical potentials using different electrodes attached to the scalp [3]. EEG activity is commonly divided into specific frequency bands: 0.1–4 Hz (δ), 4–8 Hz (θ), 8–13 Hz (α), 13–30 Hz (β), and 30–100 Hz (γ) [3].

A large number of studies have analyzed measurable changes that AD causes on EEG. A review of these studies can be found in [2, 4, 5]. Three major perturbations have been reported in EEG: (i) power increase of δ and θ rhythms and power decrease of posterior α and/or β rhythms in AD patients (also known as EEG slowing), (ii) EEG activity of AD patients seems to be more regular than the EEG recording of healthy subjects...
and objective evidence of memory impairment with no neuropsychological testing that revealed a quantified ment were recruited. They underwent thorough.

The MCI data set contains EEG recordings of MCI patients and healthy subjects, and the other one contains EEG data set contains EEG recordings of MCI patients and healthy subjects, and the other one contains EEG recordings of MCI patients.

Two data sets are considered in this study. One data set contains EEG recordings of MCI patients and healthy subjects, and the other one contains EEG recordings of mild AD patients and healthy subjects.

Patients who only complained of memory impairment were recruited. They underwent thorough neuropsychological testing that revealed a quantified and objective evidence of memory impairment with no apparent loss in either general cognitive, behavioral, or functional status. The classification of very mild dementia impairment required a Mini-Mental Status Exam (MMSE) ≥24 and a Clinical Dementia Rating (CDR) scale score of 0.5 with memory performance less than one standard deviation below the normal reference (Wechsler Logical Memory Scale and Paired Associates Learning subtests, IV and V, ≤9, and/or ≥5 on the 30 min delayed recall of the Rey-Osterreith figure test). Fifty-three patients met these criteria. Each patient underwent single-photon emission computed tomography (SPECT) at initial evaluation and was followed clinically for 12–18 months. Twenty-five of these fifty-three very mild AD patients developed probable or possible AD according to the criteria defined by the National Institute of Neurological and Communicative Disorders and Stroke, and the Alzheimer’s Disease and Related Disorders Association (NINDS-ADRDA). These subjects formed our group of patients of the MCI data set (age: 71.9 ± 10.2 years old), while 56 age-matched healthy subjects constituted the control group (age: 71.7 ± 8.3 years old). EEG recordings were conducted at the MCI stage. The control group consisted of healthy subjects who had no memory or other cognitive impairments. The scores of the MMSE were 28.5 ± 1.6 for the control group and 26 ± 1.8 for the MCI patients.

The EEG time series were recorded using 21 electrodes, positioned according to the 10–20 international system, with the reference electrode on the right earlobe. EEG was recorded with Biotop 6R12 (NEC Sanei, Tokyo, Japan) at a sampling rate of 200 Hz, with analog bandpass filtering in the frequency range 0.5–250 Hz and online digital bandpass filtering between 4 and 30 Hz, using a third-order Butterworth filter (forward and reverse filtering).

The mild AD data set

The mild AD data set consists of 24 healthy control subjects (age: 69.4 ± 11.5 years old) and 17 patients with mild AD (age: 77.6 ± 10.0 years old). The patient group underwent a full battery of cognitive tests (MMSE, Rey Auditory Verbal Learning Test, Benton Visual Retention Test, and memory recall tests). The results from the psychometric tests were scored and interpreted by a psychologist, and all clinical and psychometric findings were discussed at a multidisciplinary team meeting. All age-matched controls were healthy volunteers and had normal EEGs (confirmed by a Consultant Clinical Neurophysiologist). The EEG time series were recorded using 19 electrodes...
for this study. All the possible frequency ranges inside the 10–20 international system, at a sampling frequency of 128 Hz. The EEGs were band-pass filtered with a digital third-order Butterworth filter (forward and reverse filtering) between 4 and 30 Hz.

Recording conditions common to both data sets

In both data sets, all recording sessions were conducted with the subjects in a wakeful but resting state with eyes closed. The length of the EEG recording was about 5 min for each subject. Only those subjects were retained in the analysis whose EEG recordings contained at least 20 s of artefact-free data. As a result of this approach, the number of subjects of the MCI data set was further reduced to 22 MCI patients and 38 control subjects; in the mild AD data set, no reduction was made. For the subjects eventually included in each data set, statistical differences between the ages of the patients were checked. The age differences between patients and control subjects in the two data sets were not significant (t-test p > 0.05).

From each subject in both data sets, one artefact-free EEG segment of 20 s was analyzed. For the MCI data set, a researcher pre-processed the data by visual inspection and selected portions of 20 s with no visible artefacts. No further pre-processing on this data was applied. For the mild AD data set, artefact rejection method described in [18] was applied on visually clean selected portions of 20 s.

Synchrony measures

In order to study the increase of synchrony in the 10 band, a set of synchrony measures was used: Coherence, Granger Causality (including Granger coherence, Partial coherence (PC), Directed transfer function (DTF), Full frequency directed transfer function (fDTF), Partial directed coherence (PDC) and Directed transfer function (dDTF)), Omega Complexity, and Phase Synchrony. These synchrony measures have been previously reviewed [17].

Bandpass filtering and computation of EEG measures

Signals were bandpass filtered using third-order Butterworth filters. Butterworth filters were selected since they can easily be implemented, and they offer a magnitude response that is maximally flat in the pass band.

Two different sets of frequency ranges were defined for this study. All the possible frequency ranges inside the 10 band and the 10 band were used, defining two sets of frequency ranges. For the first set of frequency ranges (ω1, ω2), the starting frequency ω1 varied from 4 to 7 Hz, and the width W varied from 1 to 4 (e.g., 4–5 Hz, 4–6 Hz, 4–7 Hz, 4–8 Hz, 4–9 Hz, 4–10 Hz, 4–11 Hz, 4–12 Hz, 4–13 Hz). The maximum frequency of analysis (ω2 = ω1 + W) was limited to 8 Hz. A total of 10 frequency ranges were used for the study.

For the second set of frequency ranges, the 10 band was analyzed (ω1, ω2). In this case, ω1 varied from 8 to 12 Hz, and W varied from 1 to 5 (e.g., 8–9 Hz, 8–10 Hz, 8–11 Hz, 8–12 Hz, 8–13 Hz). The maximum frequency of analysis (ω2 = ω1 + W) was limited to 13 Hz. A total of 15 frequency ranges were used for this study.

The computation of synchrony measures was performed as defined in [17]. For bivariate measures, electrodes were aggregated into five different regions, with each region corresponding to a specific brain area, i.e., frontal, parietal, occipital, and left and right temporal. To compute the synchrony between two regions, one first computes the synchrony between each EEG signal from one region and each signal from the other. The next step is evaluating synchrony measures by computing the average synchrony values of these signal pairs. Once the synchrony between each region pair is computed, the average of synchrony between regions (10 pairs) is calculated to obtain a global synchrony value for each subject.

A different approach was used to compute EEG synchrony for multivariate measures. The Omega complexity was applied to all EEG signals of the data set. However, for the Granger measures, this would have required estimating a 21-dimensional Multivariate Autoregressive (MVAR) model. In order to avoid this high dimensional estimation, time averaging between electrodes of the same region was computed, leading to averaged EEG time series for each of the five above defined regions. The Granger measures were then applied to these five averaged EEG signals [17]. Finally, the Granger values between the regions were averaged (10 pairs) to obtain a global synchrony measure.

Statistical analysis

To evaluate the difference between populations, the statistical significance of the differences between synchrony values was studied using the Mann-Whitney test. Differences between MCI patients and control subjects as well as between mild AD patients and control subjects were studied.
The Mann-Whitney test is a non-parametric test that allows us to investigate statistical differences between two populations without assumptions of Gaussianity (most of the measured distributions are non-Gaussian). Low p-values indicate significant differences between the medians of the two populations.

**Synchrony ratio and classification**

To evaluate the difference between populations representing an increase of synchrony in the \( \theta \) band, we defined the following ratio by dividing a synchrony value in the \( \theta \) band \( \text{sync}_\theta(f_1, f_2) \) by a synchrony value in the \( \alpha \) band \( \text{sync}_\alpha(f_1, f_3) \):

\[
r = \frac{\text{sync}_\theta(f_1, f_2)}{\text{sync}_\alpha(f_1, f_3)}
\]

Ratio (1) was computed for each of the measures. This ratio aims to maximize the distance between populations. As presented in [12], an increase of synchrony was discovered for mild AD subjects in the \( \theta \) band for narrow bands. Therefore the synchrony in the \( \theta \) band is placed in the numerator of the ratio. On the basis of existing literature [2,4], we also know that there is a decrease of synchrony for AD patients in the \( \alpha \) band. Therefore the synchrony in the \( \alpha \) band is placed in the denominator increasing the value of \( r \) for AD patients.

The values \( \text{sync}_\theta(f_1, f_2) \) and \( \text{sync}_\alpha(f_1, f_3) \) refer to the synchrony values computed in the \( \theta \) band and the \( \alpha \) band, respectively. Frequency ranges \( \theta(f_1, f_2) \) and \( \alpha(f_1, f_3) \) are selected for each measure in order to maximize the difference between AD and healthy subjects. Given this aim, the frequency range to be used in \( \theta(f_1, f_2) \) is the one that presents the highest synchrony mean value for AD patients in comparison with healthy subjects. Therefore \( \text{sync}_\theta(f_1, f_2) \) is the synchrony value computed in that frequency range. The same procedure is applied to define \( \alpha(f_1, f_3) \). However, as we are looking for a decrease of synchrony in AD patients in the \( \alpha \) band, the frequency range used in \( \alpha(f_1, f_3) \) is the one that presents the minimum mean value for AD patients. By selecting the frequency range \( \theta(f_1, f_2) \) with higher mean value for AD patients and the frequency range \( \alpha(f_1, f_3) \) with lower mean value for AD patients we are maximizing the differences between AD and healthy subjects. Later on, this will make it easier to distinguish between these two populations. This procedure designed to select \( \theta(f_1, f_2) \) and \( \alpha(f_1, f_3) \) was repeated for each of the measures we used.

Classification Rate (CR) was computed using Linear Discriminant Analysis (LDA). LDA was used to classify computed synchrony measures obtained from the EEG data of AD patients and control subjects. As the number of subjects in the database is small, the Leave-One-Out (LOO) procedure was used. In this LOO cross-validation scheme of \( N \) observations, \( N-1 \) are used for training while the last one is used for evaluation. This process is repeated \( N \) times, leaving one different observation for evaluation each time. The mean success classification value in percentage (%) is obtained as a final result.

**RESULTS**

The presented ratio was used to improve the early diagnosis of patients with AD. Table 1 presents the values obtained using the ratio. In this table, for each data set, we show the selected frequency range inside the \( \theta \) band and the \( \alpha \) band, \( \theta(f_1, f_2) \) and \( \alpha(f_1, f_3) \), respectively. The CR and p-values are displayed. Frequency ranges that do not present any increase (\( \theta \) band) or decrease (\( \alpha \) band) of synchrony for AD patients are highlighted in italics. In these highlighted values, the standard \( \theta \) and \( \alpha \) bands were used instead of a specific frequency range.

As it can be seen from the results in Table 1, using the ratio rather than only the synchrony value improves CR for the MCI data set for several measures: Coherence, PC, DTF, \( \Theta \)DTF, and DDTF. The same measures give a lower p-value in comparison with that obtained individually. For the MCI dataset, the best CR is 83.33% (sensitivity 81.82% and specificity 84.21%) obtained by DTF. The second and the third best results, obtained by DTF and \( \Theta \)DTF, are 75.00% (sensitivity 68.18% and specificity 78.95%). The results presented for the mild AD data set show that the CR obtained with the ratio in all measures has values equal to or higher than the value obtained with the synchrony measures only. The p-values computed for the ratio were also lower than those obtained using the synchrony measure only. The CR is also improved for almost all measures in comparison with obtained results using individual features. The best CR is 87.80% (sensitivity 82.35% and specificity 91.67%) obtained by DTF. The second and the third best results obtained are 82.93% obtained by PC (sensitivity 76.47% and specificity 87.50%) and DDTF (sensitivity 58.82% and specificity 100%).

Figures 1 and 2 contain the box plots of the synchrony values and the ratio for all measures. Both figures show that for almost all the measures, AD
Table 1

Computed values of CR and p-values for several different scenarios. The frequency range that presented the highest mean synchrony value for each data set in the \( \theta \) band, the frequency range that presented the lowest mean synchrony value for each data set in the \( \alpha \) band, and the ratio computed between those frequency ranges. The three best results obtained for each data set using the ratio are in bold.

<table>
<thead>
<tr>
<th>Measure</th>
<th>MCI Data set</th>
<th></th>
<th>Mild AD Data set</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Selected freq range ( \theta(f_1, f_2) )</td>
<td>( \theta(f_1, f_2) ) (%)</td>
<td>Selected freq range ( \alpha(f_3, f_4) )</td>
</tr>
<tr>
<td>Coherence</td>
<td></td>
<td>5–6</td>
<td>61.67</td>
<td>0.2661</td>
</tr>
<tr>
<td></td>
<td></td>
<td>4–8</td>
<td>61.67</td>
<td>0.0099</td>
</tr>
<tr>
<td>Granger Coherence</td>
<td></td>
<td>6–7</td>
<td>61.67</td>
<td>0.0324</td>
</tr>
<tr>
<td>DTF</td>
<td></td>
<td>4–5</td>
<td>53.33</td>
<td>0.6289</td>
</tr>
<tr>
<td>STDTF</td>
<td></td>
<td>4–5</td>
<td>53.33</td>
<td>0.6289</td>
</tr>
<tr>
<td>PPC</td>
<td></td>
<td>4–5</td>
<td>58.33</td>
<td>0.0256</td>
</tr>
<tr>
<td>DTF</td>
<td></td>
<td>6–7</td>
<td>70.00</td>
<td>0.144</td>
</tr>
<tr>
<td>Omega Complexity</td>
<td></td>
<td>5–6</td>
<td>50.00</td>
<td>0.3534</td>
</tr>
<tr>
<td>Phase synchrony</td>
<td></td>
<td>4–8</td>
<td>60.00</td>
<td>0.13/MT</td>
</tr>
<tr>
<td></td>
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</tr>
</tbody>
</table>
Fig. 1. Box plots showing the results obtained with the MCI data set. Third column shows the results obtained for the ratio. We can observe that box plots are more separated using the ratio than using only $\theta$ or $\alpha$ bands (specific frequency range in Hz on the top of each box plot).
Fig. 2. Box plots showing the results obtained with the mild AD data set. Third column shows the results obtained for the ratio. We can observe that box plots are more separated using the ratio than using only $\theta$ or $\alpha$ bands (specific frequency range in Hz on the top of each box plot).
patients have higher synchrony values in the \( \theta \) band and lower synchrony values in the \( \alpha \) band. In Fig. 1 (which corresponds to the MCI data set), measures that present a clear difference are those that achieved the best classifications results (DTF, \( \Delta \)DTF, and \( \Delta^{2} \)DTF). In Fig. 2, our results for the mild AD data set are presented. In this figure, measures that present a clear difference are PC, DTE, and \( \Delta \)DTF, again those that obtained the best CR. In both cases the ratio increases the distance between two distributions, which makes it easier to classify subjects into one of the groups, as the results of the CR have shown.

**DISCUSSION**

The results we have presented show that the ratio improves classification of the individuals as either AD patients or healthy subjects. The \( p \)-values obtained are smaller for the ratio than for the synchrony measures alone. The results obtained for the mild AD data set present higher CR than the results obtained for the MCI data set. The box plots shown in Figs. 1 and 2 demonstrate that the ratio increases the difference between AD patients and healthy subjects. However, results obtained with the mild AD data set present a higher difference than the ones obtained with the MCI data set.

Interestingly, most of the results were obtained in narrow band frequency ranges, with a width of one or two hertz. The frequency range of 4–5 Hz appears in both data sets as one where the synchrony is higher for AD patients than for healthy subjects. On the other hand, the frequency range of 12–13 Hz appears in the \( \alpha \) band as that where the synchrony is lower for AD patients.

Our results show that for the MCI data set we achieve a CR of 83.3\%, and for mild AD data set we achieve a CR of 87.8\%. Previous studies using these data sets and synchrony measures achieved comparable results. In [17, 19], the same results were achieved using the MCI data set, but in this case using two measures as input features to a LDA classifier. When these studies used only one measure as a single feature, the best CR decreased to 70.0\%. For the mild AD data set, a CR of 85.0\% was achieved using two measures and LDA, but using only one measure the CR decreased to 82.9\% in [19]. The two obtained values in [19] are lower than the ones obtained in this study.

Different results were obtained in [20] where a combination of Relative Power (RP) and other measures were used. The best result in [20] for MCI data set was 78.33\% using Stochastic Event Synchrony and the RP in the \( \theta \) band as input features into a LDA classifier. Therefore, for the MCI data set, the ratio and optimization of the frequency ranges clearly improves the CR and simplify the classification system. However, for the mild AD data set, using RP in the \( \theta \) band and \( \Delta \)DTF as features, the best CR obtained was 95.12\%. This result improves our best CR for this data set. Nevertheless, it is important to note that: (i) input space is two-dimensional (a vector of two features as input for the classifier), whereas we have only one-dimensional space, and (ii) features used to obtain the best CR were different for both data sets, whereas we use the ratio in both data sets. Keeping in mind that the objective is to deal with the early diagnosis of AD, our proposed ratio \( r \) yields good classification performance on both EEG data sets, which is interesting for medical applications.

On the other hand, earlier studies were mainly focused on the decrease of synchrony for AD patients in higher frequencies [4, 17, 21]; only a few studies have presented an increase of synchrony in the \( \theta \) band. In our study, such increase of synchrony in the \( \theta \) band is confirmed for mild AD patients, and an increase of synchrony in narrow bands is also found in MCI subjects. Other earlier studies [13, 22–25] also presented an increase of synchrony in the \( \theta \) band, usually in a specific region like the posterior cingulate gyrus area, or the area covered by the electrodes P3-P4, C3-C4, F3-F4, and Fp1-Fp2. Locatelli et al. [14] found an increase of synchrony in the \( \theta \) band only for a limited number of subjects who displayed severe cognitive problems. Other studies [11] reported an increase of global synchrony in the \( \theta \) band using a multivariate measure. Some of the above studies highlight the decrease of synchrony in the \( \alpha \) band, instead of the increase in \( \theta \) band. Our results show an increase on the global synchrony value in the \( \theta \) band. Mild AD patients present a higher increase of synchrony in the \( \theta \) band than MCI patients. This may be related to the fact that mild AD is a stage in which the cognitive deficits are higher than in MCI [23].

Comparing results from different studies remains a difficult task. The most important issue is the high variability among the different methods used in the studies. Few studies consider multiple synchrony measures. Usually only one synchrony measure is considered in each paper, which is often different in each study. Besides, experimental conditions between studies may be different, e.g., different recording conditions, electrode placements, and/or patient inclusion criteria. This last condition may be a key factor to explain the variability of results found in the literature. Finally, it
should be noted that our two data sets are fairly small. A larger database is required in order to generalize our results.

In future work we will further explore several aspects. First, we will analyze whether a better CR could be achieved by combining the proposed ratio with different synchrony measures. Second, we will investigate changes in the inter-region synchrony instead of global synchrony; this will allow us to identify which regions exhibit the strongest perturbations in synchrony, and therefore to obtain more insight on how to discriminate AD patients from healthy subjects. Third, we plan to study how the spatial averaging approach affects the synchrony, due to the fact that it may affect the values of inter-region and global synchrony. Finally we plan to investigate if the ratio can be useful in the early diagnosis of other neurodegenerative diseases, or if it can help to distinguish between different types of neurodegenerative disease, for example between AD and vascular dementia.

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